

Theoretical overview of **low X physics with eA at an EIC**

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Aspects of low X physics with eA at an EIC

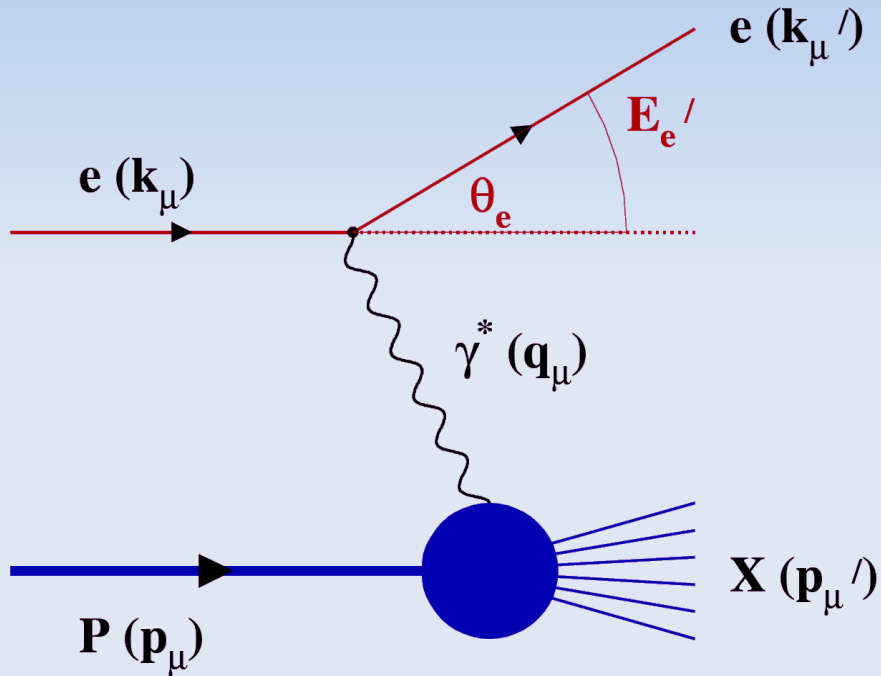
Probing extreme QCD:

unitarity, universality, strong color fields

Connection to heavy ion physics at RHIC/LHC

A hadron at small x

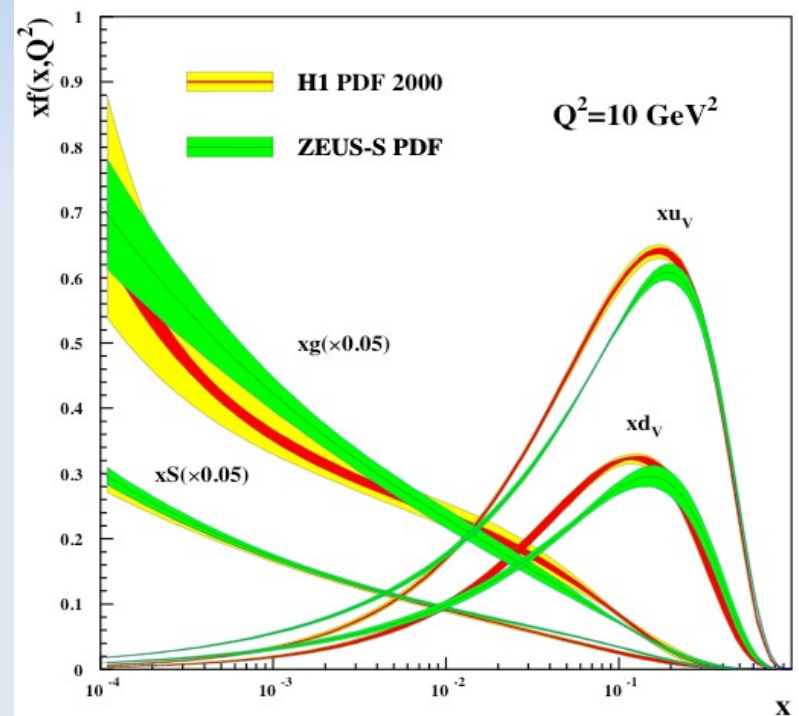
DIS: $e p \rightarrow e X$



$x = \frac{p^+}{P^+}$ is the fraction of hadron energy carried by a parton

HERA:

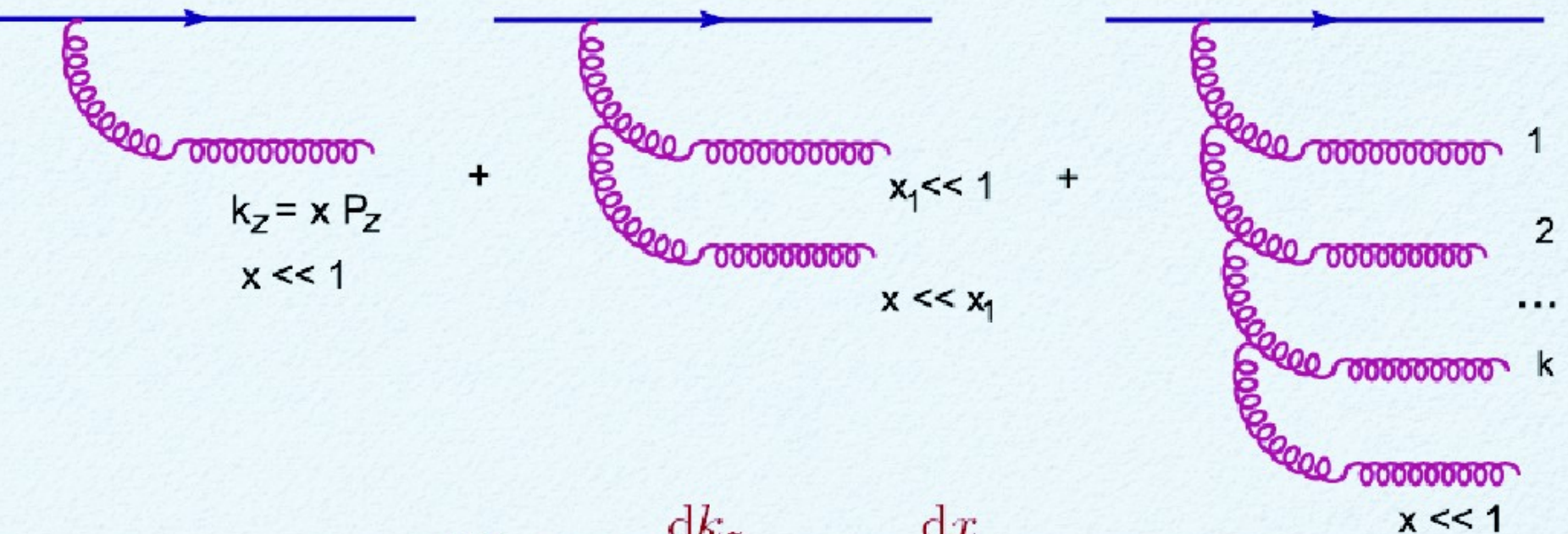
there are a lot of gluons at small x



**Q^2 evolution of PDF's:
DGLAP**

gluon radiation at small x : pQCD

The infrared sensitivity of bremsstrahlung favors the emission of 'soft' (= small- x) gluons



$$d\mathcal{P} \propto \alpha_s \frac{dk_z}{k_z} = \alpha_s \frac{dx}{x}$$

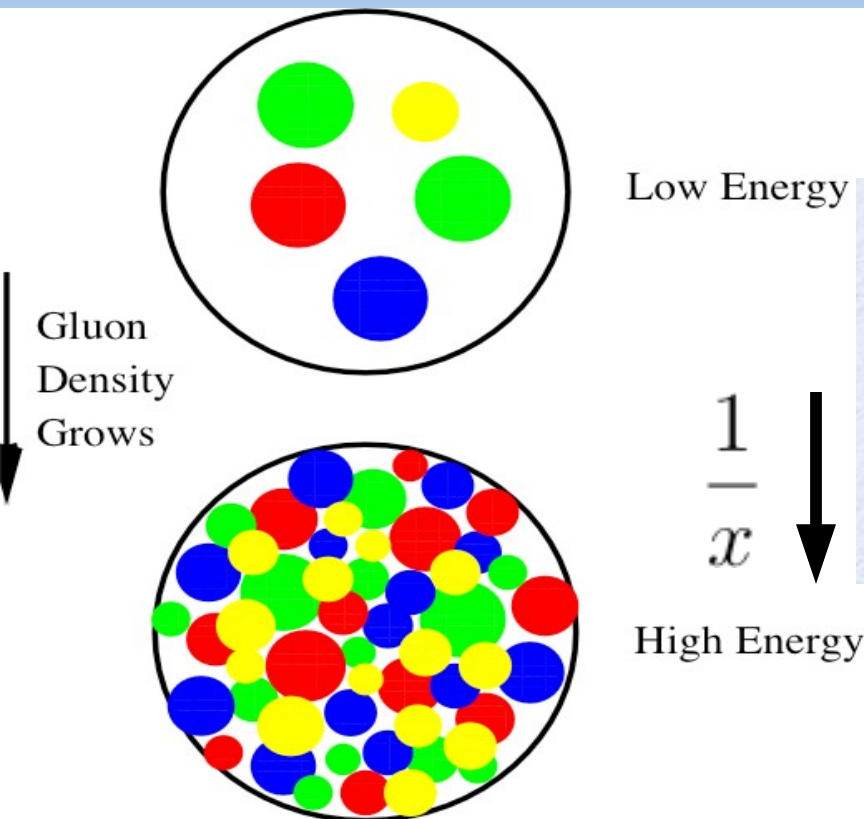
The 'price' of an additional gluon:

$$\mathcal{P}(1) \propto \alpha_s \int_x^1 \frac{dx_1}{x_1} = \alpha_s \ln \frac{1}{x}$$

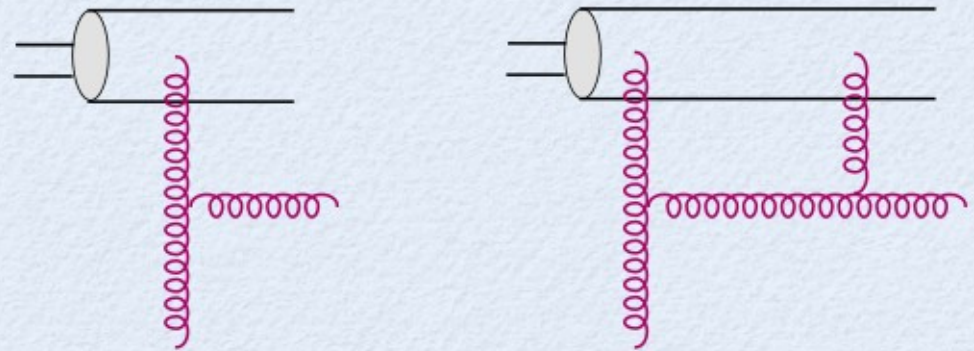
number of gluons grows fast

$$n \sim e^{\alpha_s \ln 1/x}$$

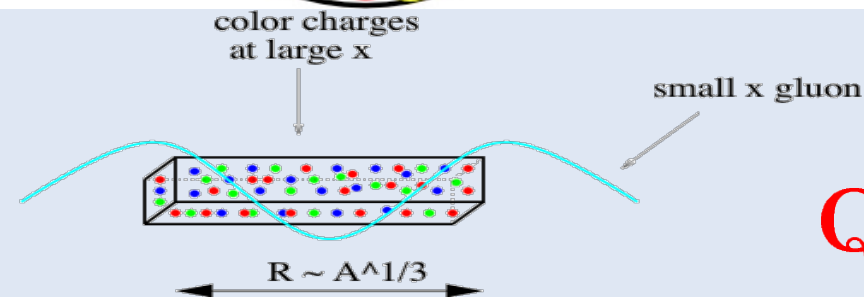
Gluon saturation



“attractive” bremsstrahlung
vs. “repulsive” recombination

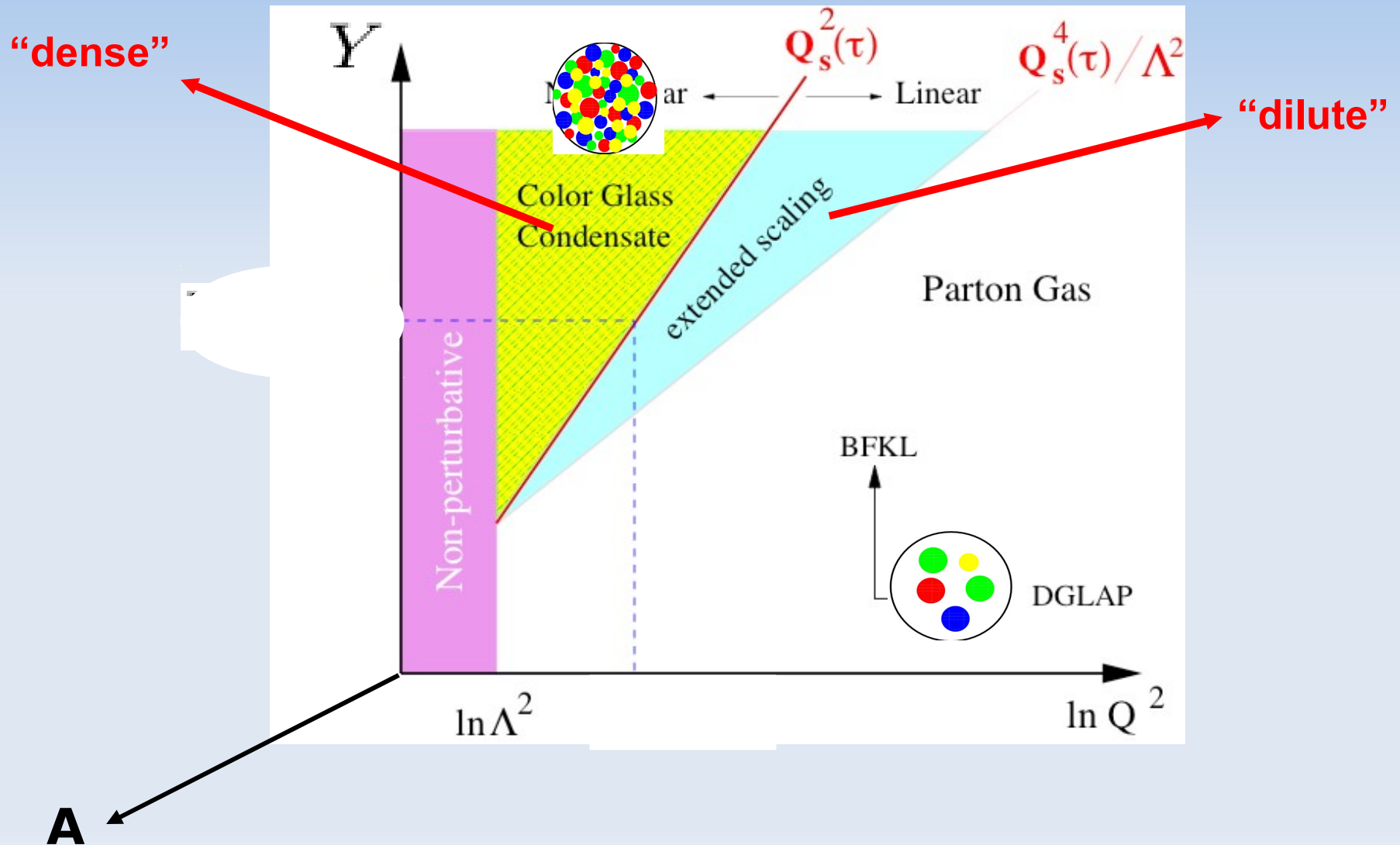


$$\frac{\alpha_s x G(x, b_t, Q^2)}{S_\perp Q^2} \sim 1$$

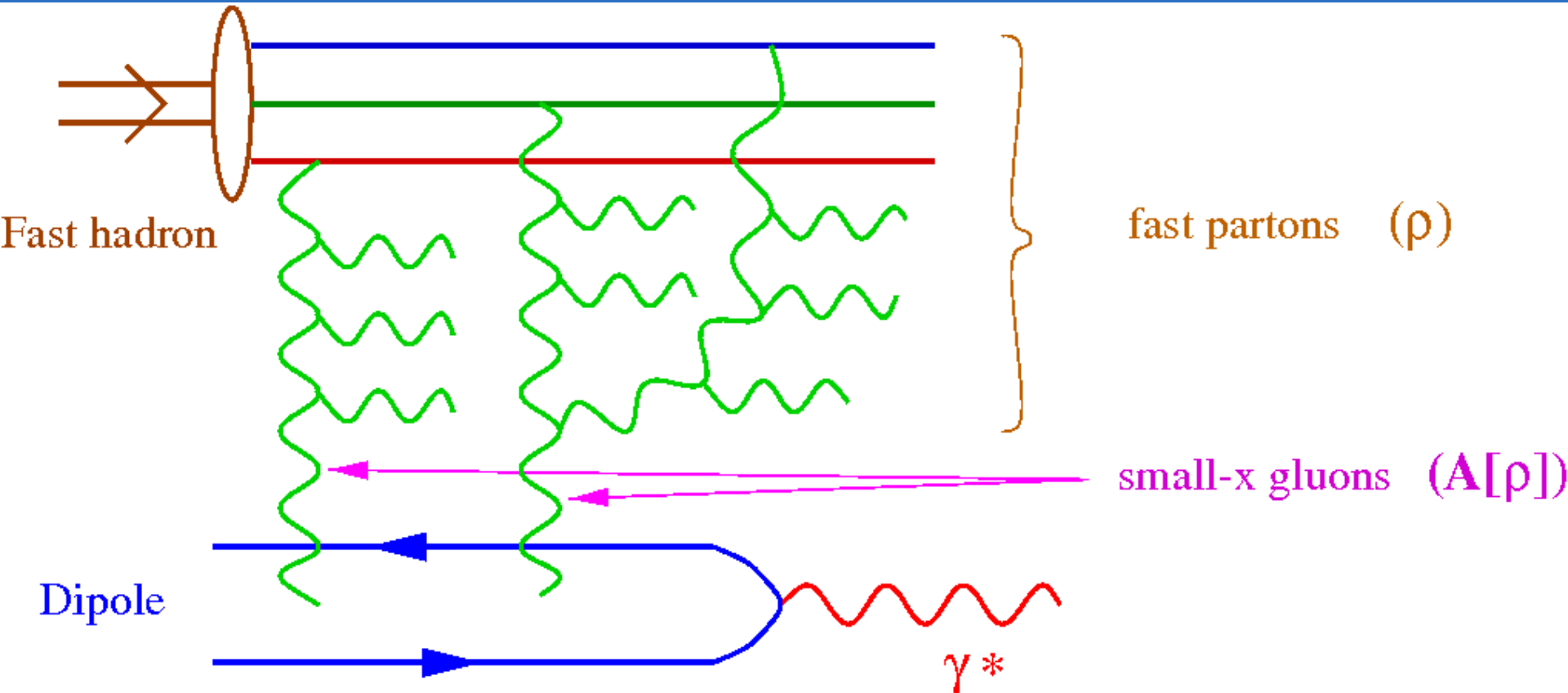


$$Q_s^2(x, b_t, A) \sim A^{1/3} \left(\frac{1}{x}\right)^{0.3}$$

Road Map of QCD Phase Space



DIS at small X: structure functions



$$F_2(x, Q^2) = \frac{Q^2}{4\pi^2 \alpha_{em}} (\sigma_T + \sigma_L)$$

$$\sigma_{T,L} = \int d^2r d\alpha \, |\Psi_{T,L}(r, \alpha, Q^2)|^2 \sigma_{dip}(x, r)$$

BK equation

$$\frac{d}{dy} \langle \text{Tr} \mathbf{V}_{\mathbf{x}}^\dagger \mathbf{V}_{\mathbf{y}} \rangle = -\frac{\bar{\alpha}_s}{2\pi} \int d^2 \mathbf{z} \frac{(\mathbf{x} - \mathbf{y})^2}{(\mathbf{x} - \mathbf{z})^2 (\mathbf{y} - \mathbf{z})^2} \times$$

$$\left[\langle \text{Tr} \mathbf{V}_{\mathbf{x}}^\dagger \mathbf{V}_{\mathbf{y}} \rangle - \frac{1}{N_c} \langle \text{Tr} \mathbf{V}_{\mathbf{x}}^\dagger \mathbf{V}_{\mathbf{z}} \rangle \langle \text{Tr} \mathbf{V}_{\mathbf{z}}^\dagger \mathbf{V}_{\mathbf{y}} \rangle \right]$$

$$S(\mathbf{y}_t, \mathbf{z}_t) \equiv \frac{1}{N_c} \langle \text{Tr} \mathbf{V}_{\mathbf{y}}^\dagger \mathbf{V}_{\mathbf{z}} \rangle$$

• Output: Modified evolution kernel:

$$\Rightarrow \text{Leading order:} \quad \frac{\partial S(\underline{x}, \underline{y}; Y)}{\partial Y} = \int d^2 z \, K^{LO}(\underline{r}, \underline{r}_1, \underline{r}_2) [S(\underline{x}, \underline{z}) S(\underline{z}, \underline{y}) - S(\underline{x}, \underline{y})]$$

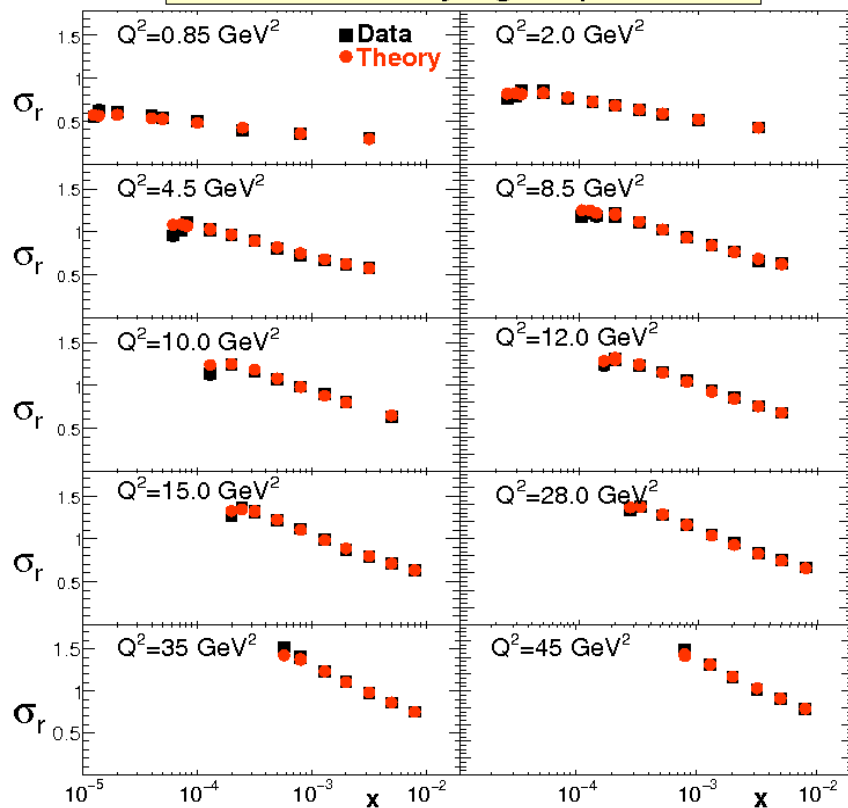
↓

$$\Rightarrow \text{Running coupling:} \quad \frac{\partial S(\underline{x}, \underline{y}; Y)}{\partial Y} = \int d^2 z \, \tilde{K}(\underline{r}, \underline{r}_1, \underline{r}_2) [S(\underline{x}, \underline{z}) S(\underline{z}, \underline{y}) - S(\underline{x}, \underline{y})]$$

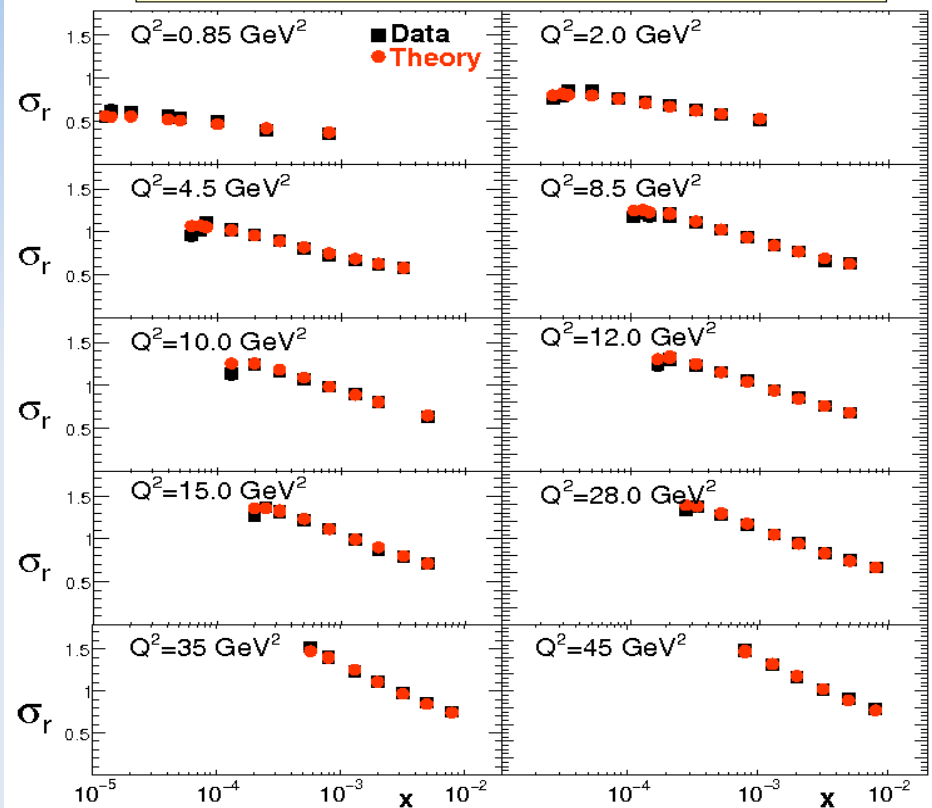
NLO: B-KW-G-BC (2007-2008)

Structure functions at HERA

Fit with only light quarks



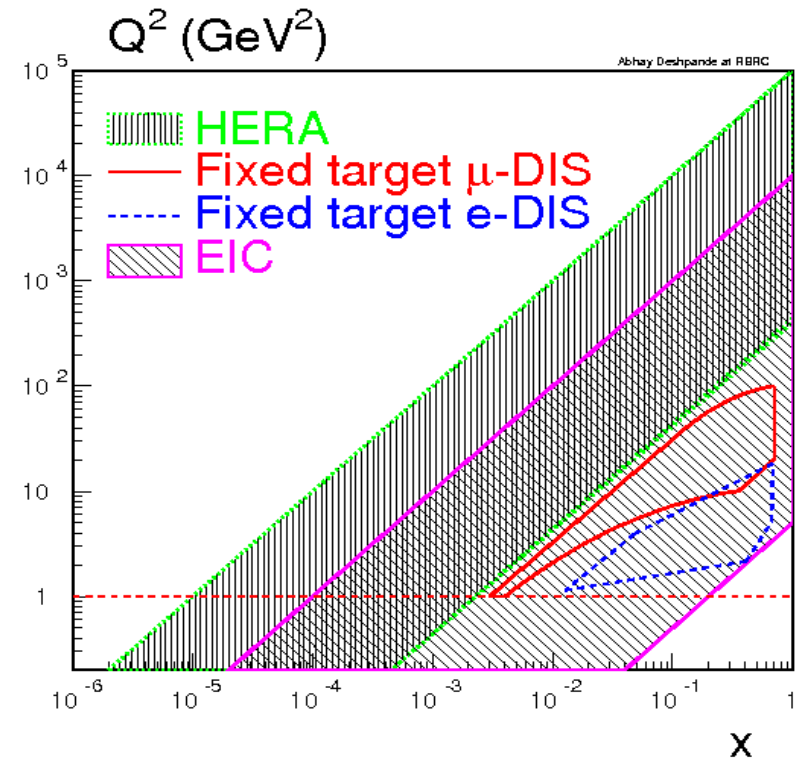
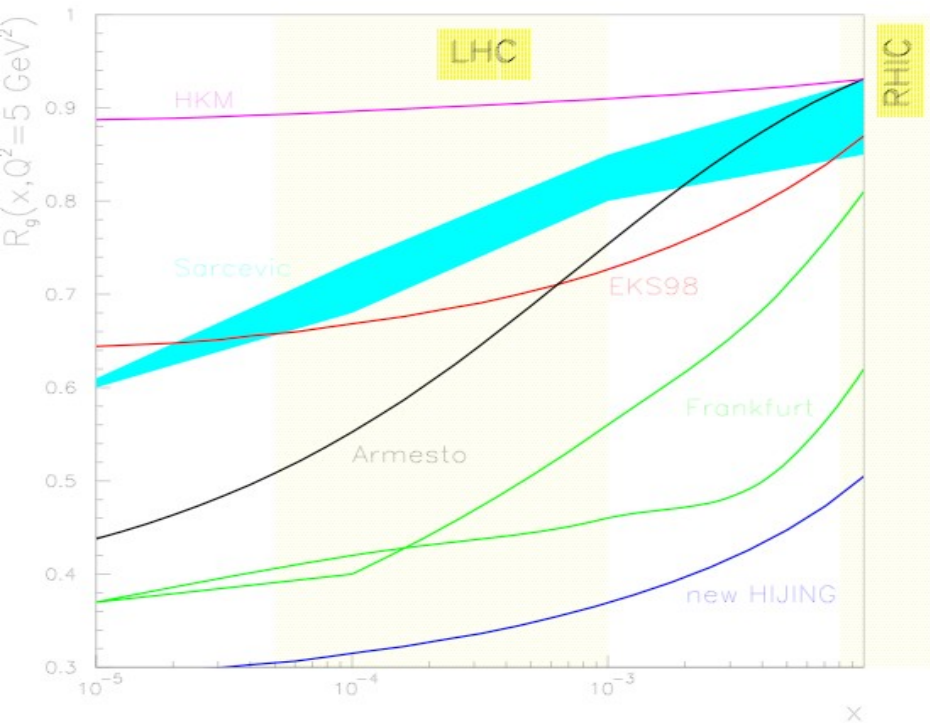
Fit including heavy quarks



AAMQS(2010)

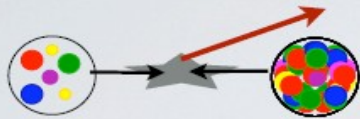
*PQCD: DGLAP-based approaches also “work” :
need more discriminatory observables*

Nuclear structure functions at EIC

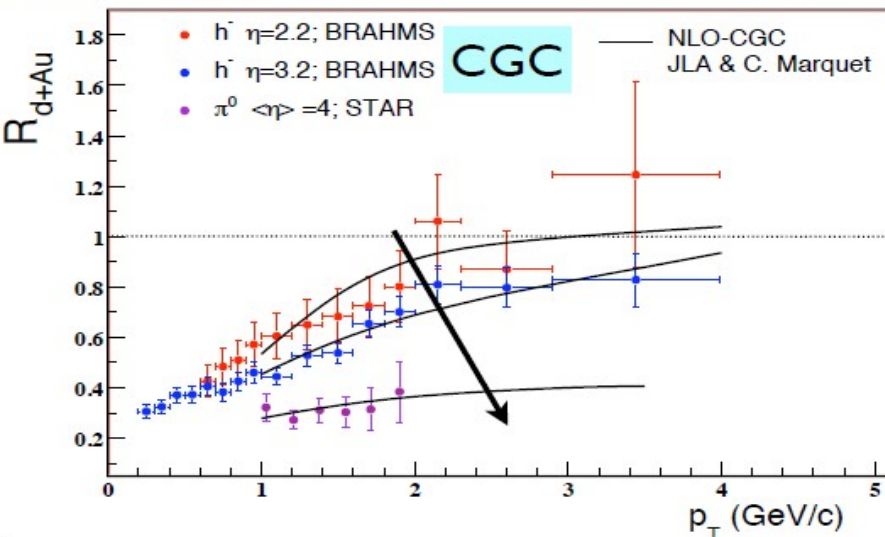


*Nuclear parton (gluon) distributions are poorly known:
severe consequences for RHIC/LHC*

RHIC d+Au data at forward rapidity

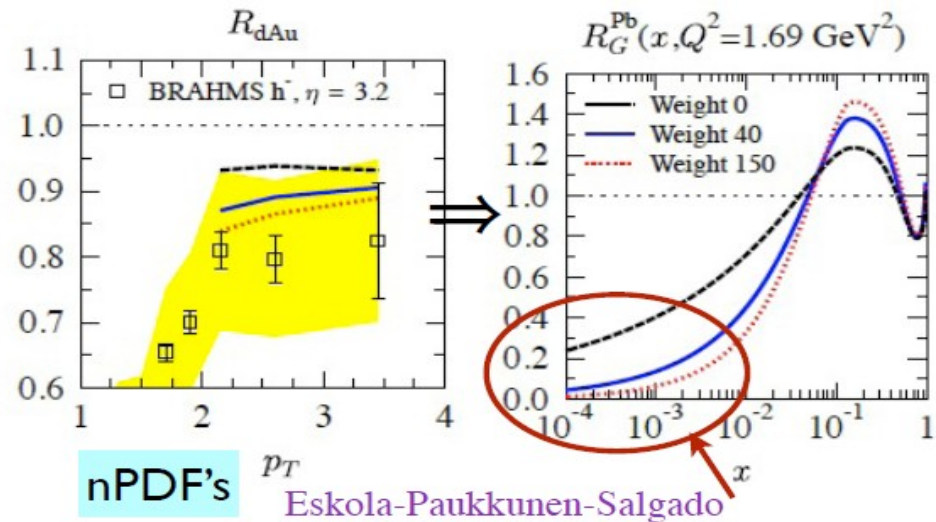


$$x_{1(2)} \sim \frac{m_t}{\sqrt{s}} \exp(\pm y_h)$$



- Forward suppression predicted and well described in the CGC framework in terms of non-linear running coupling BK evolution

How about cold matter energy loss?



- nPDF's description of forward suppression involves a huge nuclear shadowing at small- x

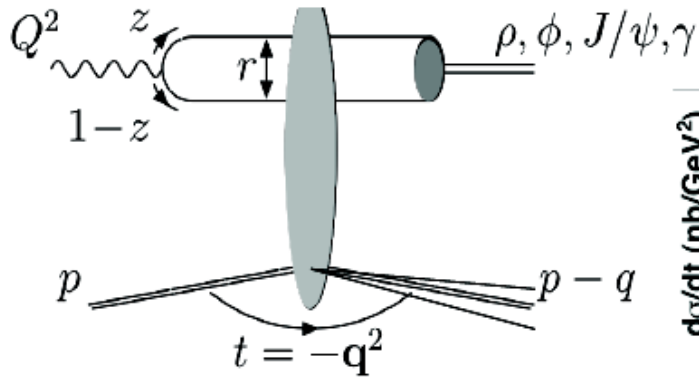
Breakdown of LT pQCD (DGLAP) ?

Diffractive structure functions: $[xg(x, Q^2)]^2$

SIDIS: *intrinsic gluon distribution function*

Diffractive vector meson production: *impact parameter dependence*

Diffractive vector meson production

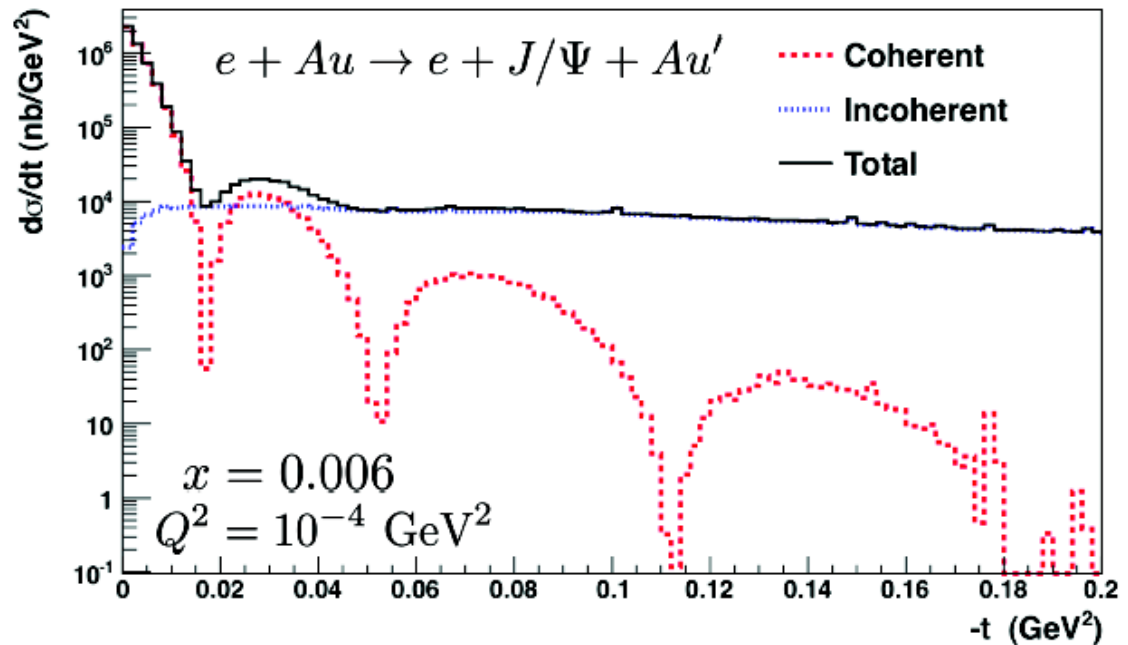


Toll and Ullrich (2011)

- as a function of t

exclusive production (coherent):
the target undergoes elastic
scattering, dominates at small $|t|$

→ steep exp. fall at small $|t|$



target dissociation (incoherent): the target undergoes inelastic scattering, dominates at large $|t|$

breakup into the nucleons

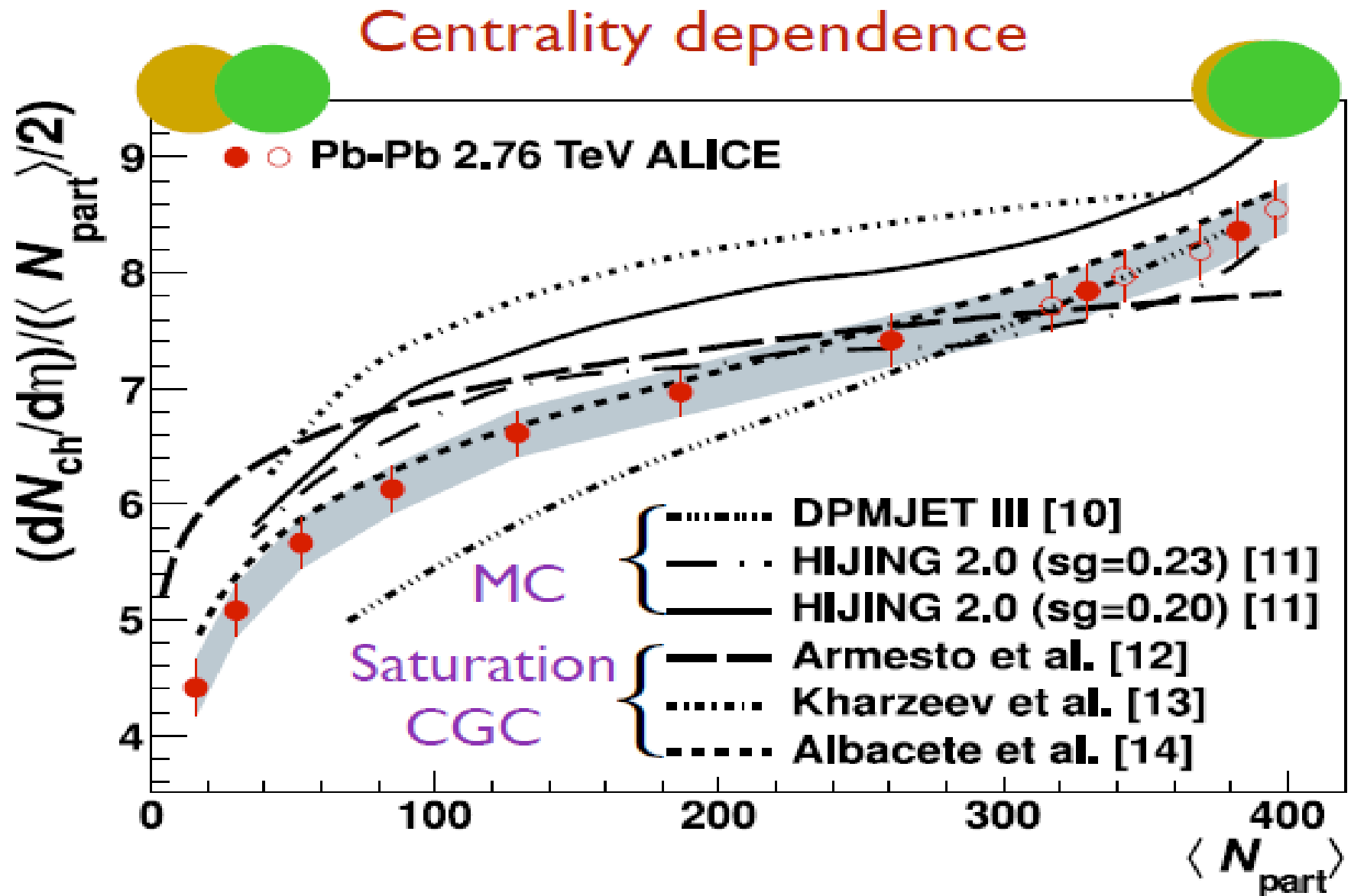
→ slower exp. fall at $0.02 < -t < 0.7$ GeV²

breakup of the nucleons

→ power-law tail at large $|t|$

Fourier transform of t dependence gives the impact parameter profile of target

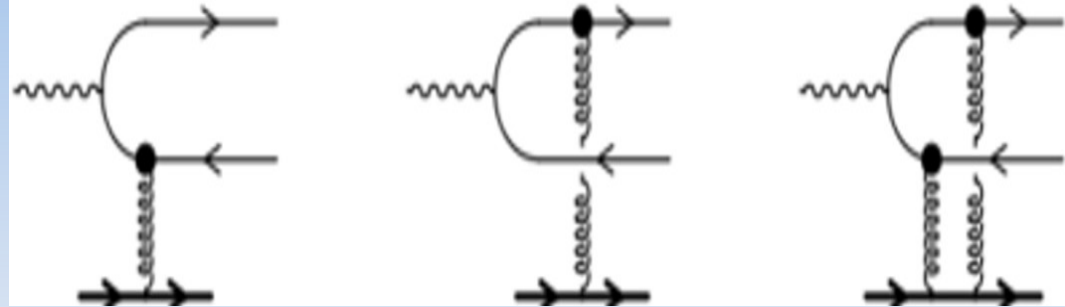
Impact parameter in AA collisions



Di-jet production: DIS

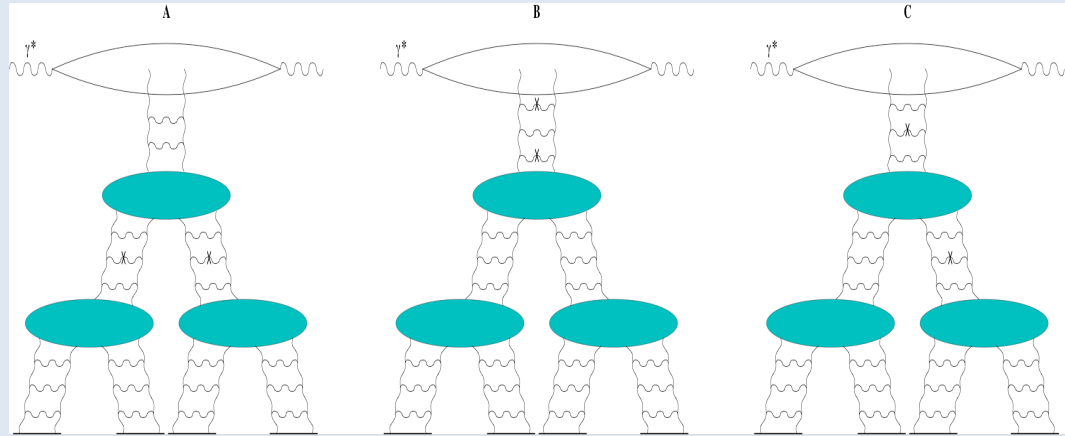
$$\gamma^* p(A) \rightarrow q \bar{q} X$$

FG & JJM, PRD67 (2003)
DMXY (2011)



$$\gamma^* p(A) \rightarrow g g X$$

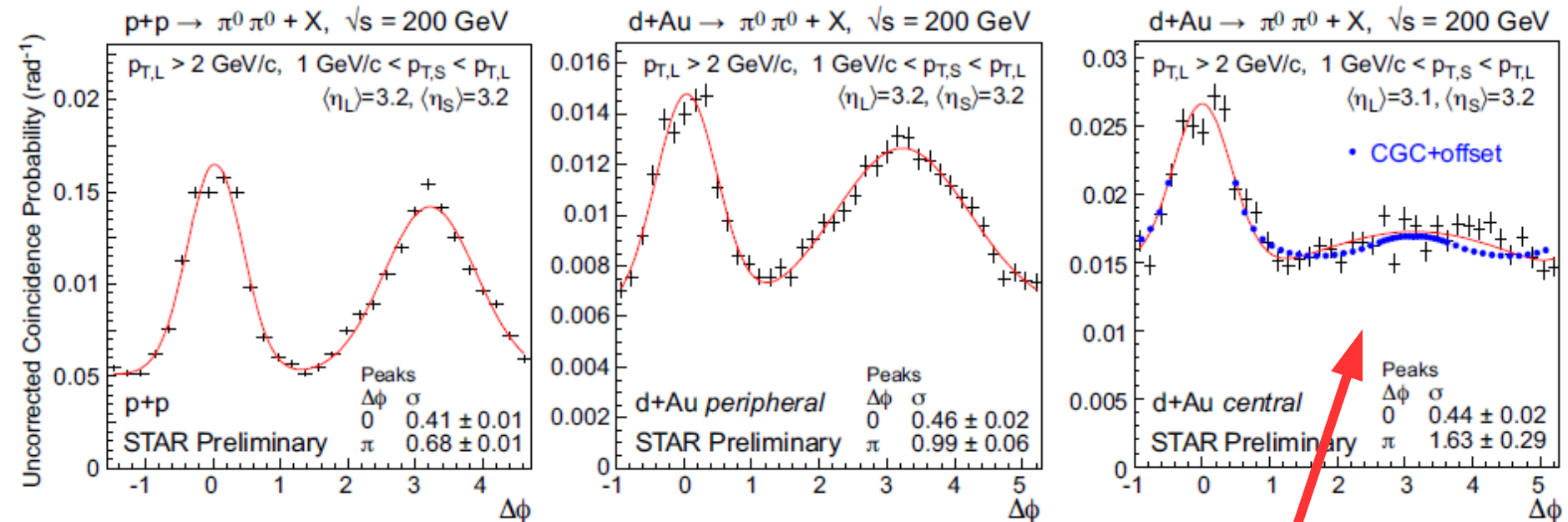
JJM & YK, PRD70 (2004)
AK & ML, JHEP (2006)



*di-jet production in DIS
probes multi-gluon correlations*

disappearance of back to back jets

Recent STAR measurement (arXiv:1008.3989v1):

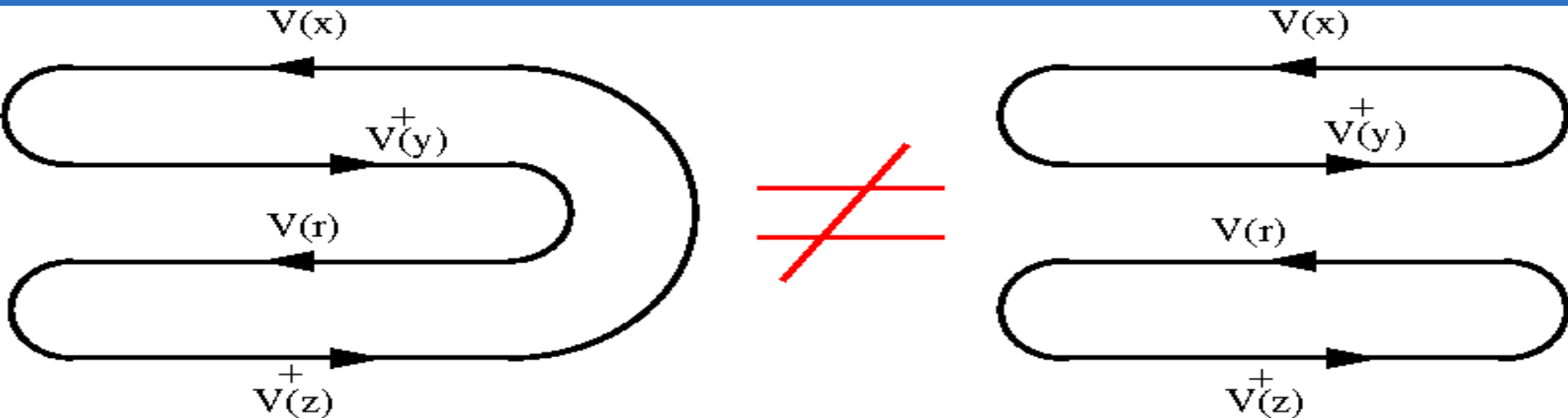


*Albacete + Marquet, PRL (2010),
Tuchin, NPA846 (2010)*

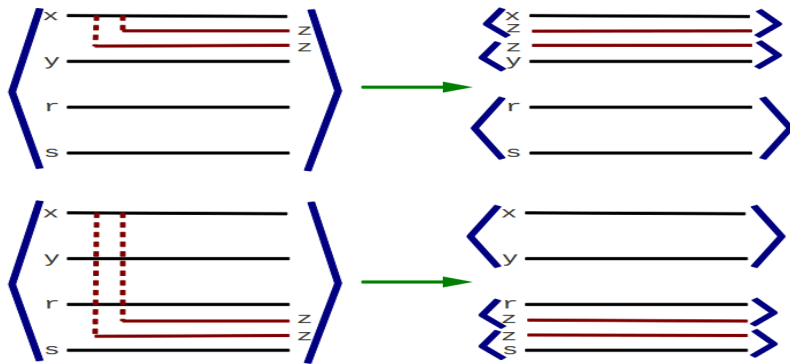
*multiple soft scatterings
de-correlate the hadrons*

**multi-gluon correlations-transverse profile of nucleus:
need to go beyond single parton distributions
(quadrupoles rather than dipoles)**

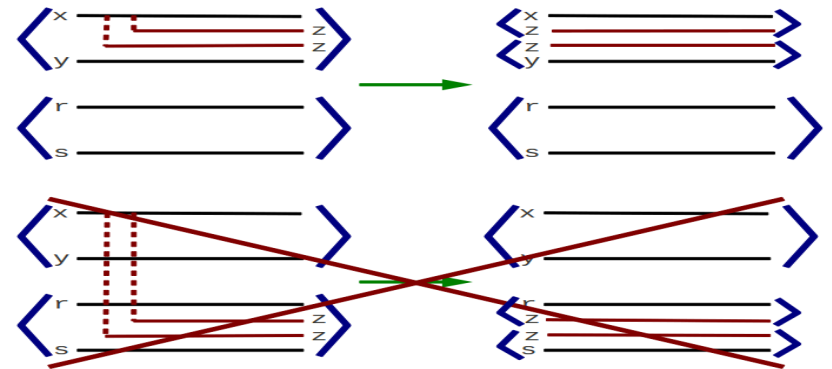
Quadrupoles vs. dipoles



and they evolve differently even at large N_c

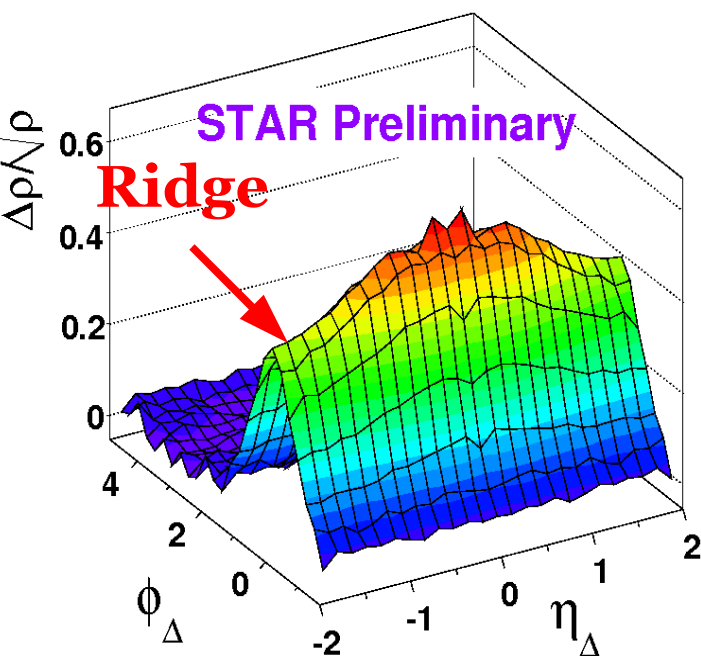


JIMWLK



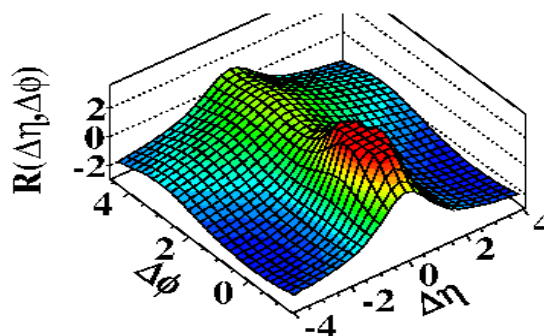
Dipole approximation

The Ridge

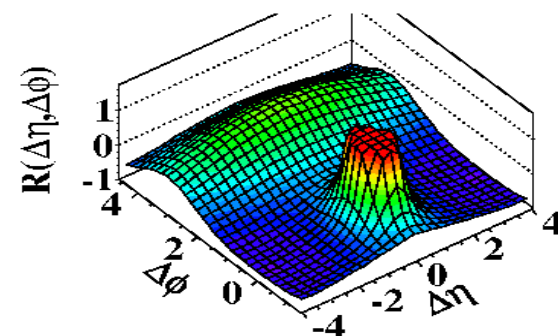


AA at RHIC

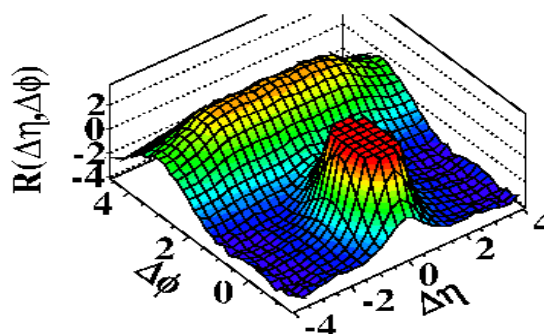
(a) CMS MinBias, $p_T > 0.1 \text{ GeV}/c$



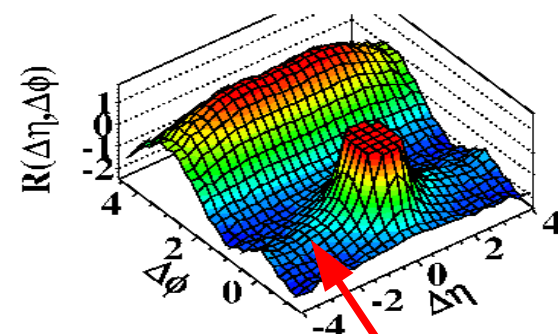
(b) CMS MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



(c) CMS $N \geq 110$, $p_T > 0.1 \text{ GeV}/c$



(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



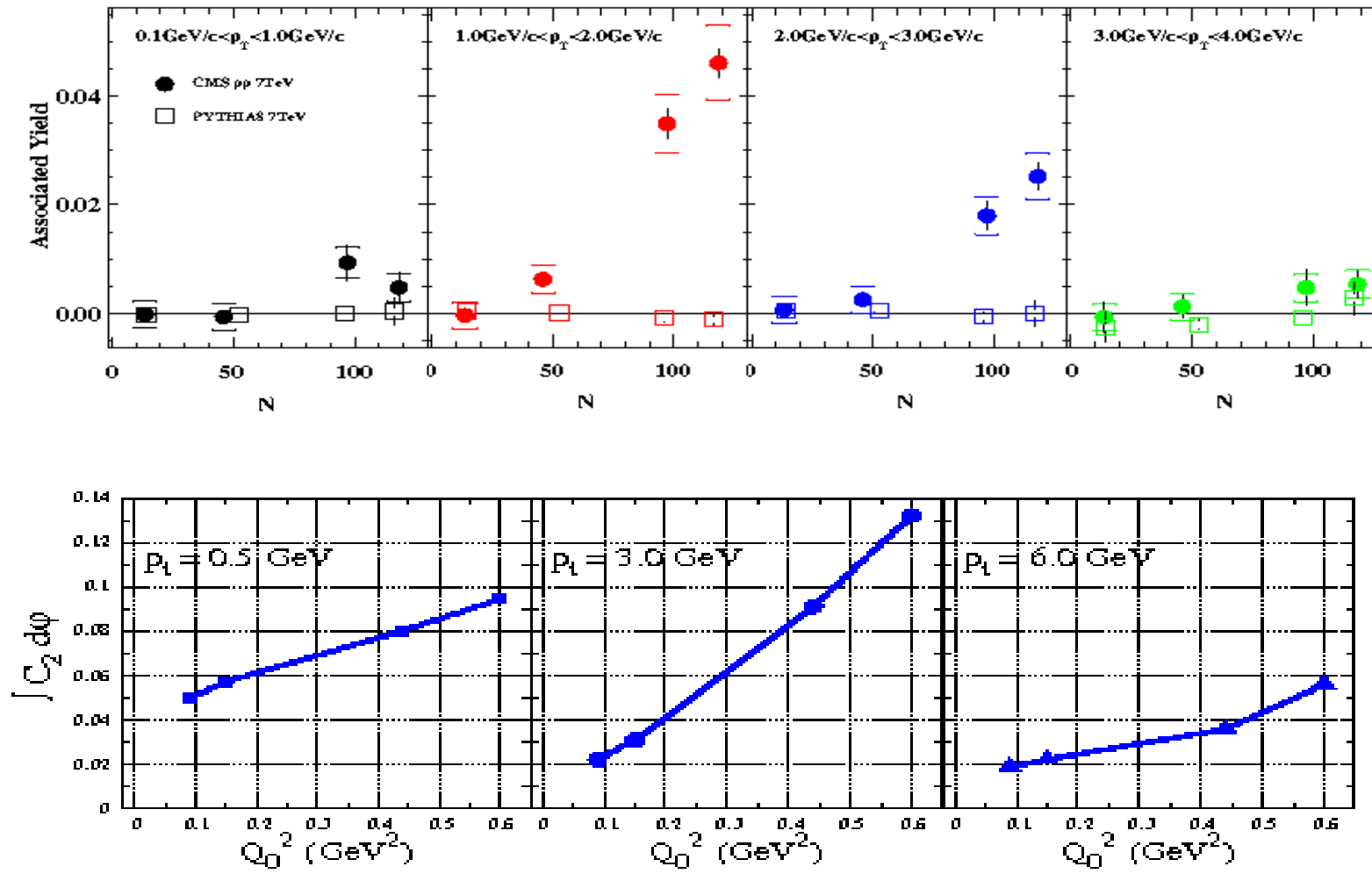
PP at LHC

long-range rapidity correlations

multi-gluon correlations in the nucleus:

need to go beyond single parton distributions

The CMS ridge at LHC



DDGJLV, PLB697 (2011) 21

The role of initial conditions

McLerran-Venugopalan (93) $\langle \mathbf{O}(\rho) \rangle \equiv \int \mathbf{D}[\rho] \mathbf{O}(\rho) \mathbf{W}[\rho]$

$$\mathbf{W}[\rho] \simeq \mathbf{e}^{-\int d^2 \mathbf{x}_t \frac{\rho^{\mathbf{a}}(\mathbf{x}_t) \rho^{\mathbf{a}}(\mathbf{x}_t)}{2 \mu^2}} \quad \mu^2 \equiv \frac{g^2 A}{S_{\perp}}$$

$$\mathbf{S}(\mathbf{y}_t, \mathbf{z}_t) \equiv \frac{1}{N_c} \langle \text{Tr} \mathbf{V}_y^{\dagger} \mathbf{V}_z \rangle \sim \mathbf{e}^{-\# (\mathbf{y}_t - \mathbf{z}_t)^2 Q_s^2}$$

how about higher order terms in ρ ?

$$\mathbf{W}[\rho] \simeq \mathbf{e}^{-\int d^2 \mathbf{x}_t \left[\frac{\rho^{\mathbf{a}}(\mathbf{x}_t) \rho^{\mathbf{a}}(\mathbf{x}_t)}{2 \mu^2} - \frac{\mathbf{d}^{\mathbf{abc}} \rho^{\mathbf{a}}(\mathbf{x}_t) \rho^{\mathbf{b}}(\mathbf{x}_t) \rho^{\mathbf{c}}(\mathbf{x}_t)}{\kappa_3} + \frac{\mathbf{F}^{\mathbf{abcd}} \rho^{\mathbf{a}}(\mathbf{x}_t) \rho^{\mathbf{b}}(\mathbf{x}_t) \rho^{\mathbf{c}}(\mathbf{x}_t) \rho^{\mathbf{d}}(\mathbf{x}_t)}{\kappa_4} \right]}$$

these higher order terms may make the spectra steeper and give leading N_c correlations (ridge)

AD+JJM+EP, in progress

Low x in eA at an EIC: extreme QCD

A new region of QCD phase space: CGC

Q_s : a dynamical semi-hard scale

multiplicities, spectra, correlations

*low x physics at RHIC (forward rapidity)
and LHC in pp , pA and AA collisions*

**EIC will enable us to probe new aspects
of low x physics in nuclei with precision**